Write your answers in the spaces provided.

You must show all of your working.

1 a and **b** are column vectors such that $\mathbf{a} = \begin{pmatrix} 8 \\ 3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} 1 \\ -7 \end{pmatrix}$. Calculate:

$$\begin{array}{c}
\text{(a) } 3a \\
3 \times \left(3\right) = \left(3 \times 8\right) \\
3 \times 3
\end{array} = \left(3 \times 8\right) = \left(3 \times 9\right)$$

.....[1]

(b) $\mathbf{a} - 4\mathbf{b}$

$$\begin{pmatrix} 8 \\ 3 \end{pmatrix} - 4 \begin{pmatrix} 1 \\ -7 \end{pmatrix}$$

$$\begin{pmatrix} 8 \\ 3 \end{pmatrix} - \begin{pmatrix} 4 \\ -28 \end{pmatrix} = \begin{pmatrix} 8 - 4 \\ 3 - -28 \end{pmatrix}$$



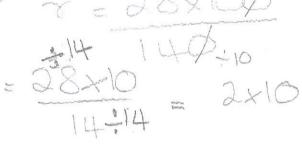
[Total 3 marks]

[2]

2 140% of x is 28. Find the value of x.

140% = 28 = 10% = 2×10 = 20

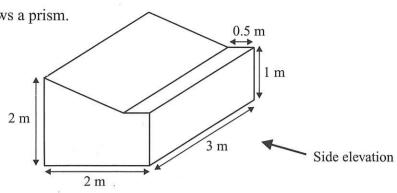
Alternate



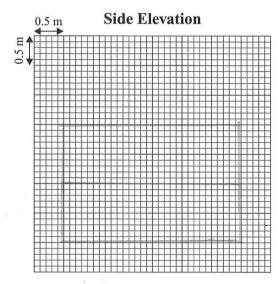
x =

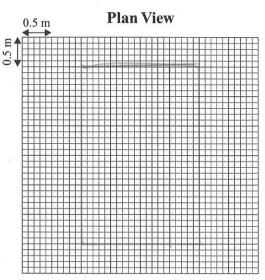
[Total 2 marks]

Leave blank 3 The diagram shows a prism.



Using the scale shown on the grids, accurately draw the side elevation and plan view of the prism.



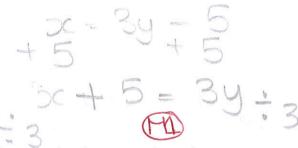


[Total 2 marks]

Leave

blank

4 (a) Make y the subject of the formula x = 3y - 5



y = 2 + 5 (1)
[2]

(b) Factorise the expression $8x^2 - 12xy$



3

1 mark for 1 correct factor

[4

[Total 4 marks]

The sets ξ , P and Q are shown below. Dom has been training for a half marathon. Leave

blank

 $\xi = \{\text{positive integers less than or equal to 20}\}\$

 $P = \{ prime numbers \}$ $Q = \{1, 2, 3, 4, 6, 8, 12\}$

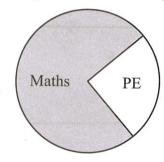
(a) List the members of the set $P \cap O$

(b) Find $n(P \cup Q)$ $U \Rightarrow union + BQ$ (PUQ) = (1, 2, 3, 4, 5, 6, 7, 8, 11, 12, 13, 17, 19)n > number in the

[2]

[Total 4 marks]

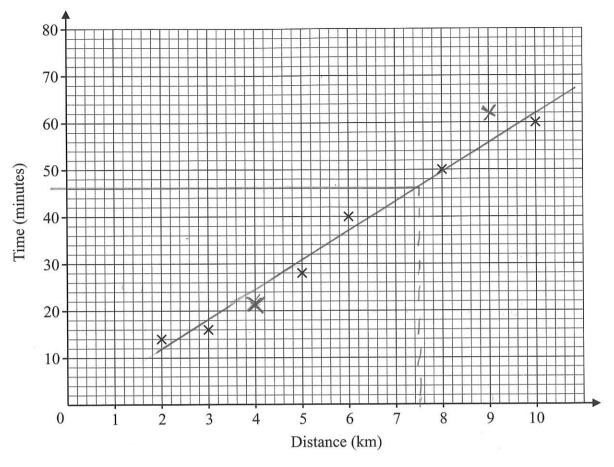
Mathilde asks her group of friends whether they like Maths, PE or History lessons the most. She puts her results in a pie chart.



She claims that, "No one in my school likes History the most." Do you agree with her statement? Explain your answer.

[Total 1 mark]

He records the distances and times taken when he goes out running.



(a) Dom also completed a 4 km run in 21 minutes and a 9 km run in 62 minutes. Plot these points on the graph.

[1]

Leave

blank

(b) Use the graph to estimate how long it would take him to run 7.5 km.

I make for line of best fit

minutes [2]

(c) Why might you not expect the points to lie in a straight line?

distance > decrease [Total 4 marks]

8 Alice has 2 dogs, Ollie and Taffy.

Ollie eats $\frac{2}{3}$ of a tin of dog food every day and Taffy eats $\frac{2}{5}$ of a tin every day. Alice buys a crate of 24 tins.

How many whole days should the crate last?

$$\frac{2}{3} + \frac{2}{5} = \frac{10}{15} + \frac{6}{15} = \frac{16}{15}$$

 $24 \div \frac{16}{15}$ $8 \div 24 \times \frac{15}{16} = 23$

Use the trick of X then fli

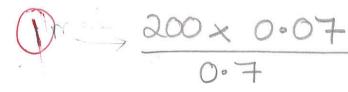
22 d

[Total 3 marks]

9 Look at this calculation.

 $\frac{226\times0.074}{0.681}$

(a) By rounding each number to 1 significant figure, work out an estimate to the calculation.



 $200 \times 0.07^{10} = 200 \times 0.7$ 0.7_{10} $= 200 \times 0.1$

(b) Explain whether you think your answer to part (a) is an overestimate, underestimate or if it is impossible to tell.

underestimate as both
numerators were rounded down
a denominator rounded up

& SO will give a smaller [1]

6

Leave blank

10 Choose an equation from the box to match each of the graphs below.

 $y = \sin x \qquad y = \cos x \qquad y = x^2 \qquad y = -x^2 \qquad y = x^3 \qquad y = -x^3$ $y = 2^x \qquad y = \frac{1}{x} \qquad y = -\frac{1}{x}$

happy face > positive quadration

 $y = \frac{2}{[1]}$

Leave

blank

(b) y 1

Just going down must be - as au answers - y values

procal > 1

y =[1]

7

then $y = \cos x$

[Total 4 marks]

(c)

(d)

A child's set of building blocks contains 5 different colours. One block is selected at random.

The table shows the probabilities of selecting a blue block and a green block.

Block Colour	Blue	Green	Orange	Red	Yellow
Probability	0.2	0.35	0.27	0.1	0.08

The probability of picking out a green or orange block is 0.62

The probability of picking out a block that is not yellow is 0.92

0.62+

Complete the table to show the probability of picking each block colour.

P/0)=0.62-0.35 = 0.270

0.90

0.52

P(not yellow) = 0.92: P(Y) = 1 - 0.92 = 0.08(1)

[Total 3 marks]

- 12 Two numbers are in the ratio 4:5.
 Their highest common factor is 16.
 - (a) Find a possible pair of numbers.

 $4 \times 16 = 64$ $5 \times 16 = 80$ I mark for each careed number

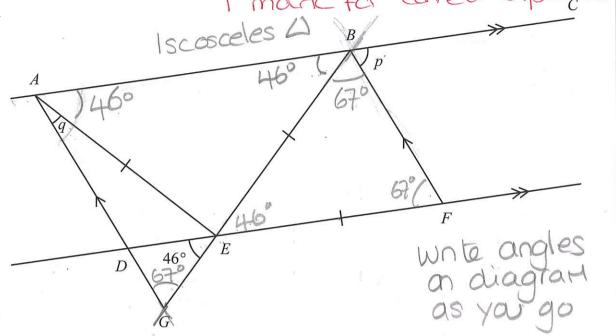
64 and 80

(b) Are there any other possible pairs? Explain your answer.

No multiples of 64 & 80 are also in ratio 4:5 but would have higher factors

[Total 3 marks]

Leave blank 13 ABC and DEF are parallel. AG and BF are parallel. AE = BE = EFAngle DEG = 46° 1 mark for p 1 mark for correct explanation blank 1 mark for 9 1 mark for correct explanation



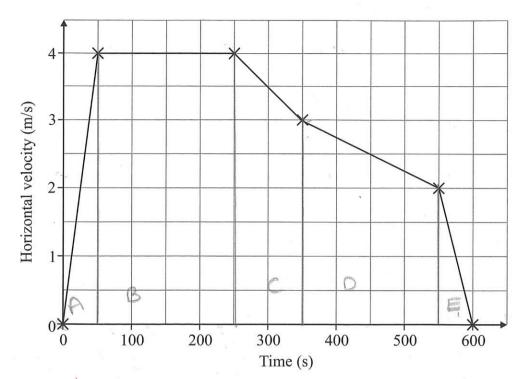
Find the size of the angles marked p and q. You must show your working.

BEF = 46° \Rightarrow opposite angles EBF & BFE are equal as iscosceles \angle $180 - 46 = 134^{\circ}$ (angles in \triangle add 180°). $134 \div 2 = 67^{\circ}$ $P = 67^{\circ}$ (AFB alternate angle) $AGE = 67^{\circ}$ (FBE atternate angle) $AGE = 67^{\circ}$ (FBE atternate angle) $AGE = 67^{\circ}$ (FBE atternate angle)

9

[Total 4 marks]

Nuala flew her drone at the beach for 10 minutes. The drone automatically recorded its horizontal velocity and Nuala was able to generate the following graph of the flight.



(a) Use the graph to work out the total horizontal distance covered by the drone.

A =
$$60 \times 4 \div 2 = 100m$$

B = $200 \times 4 = 800m$

C = $(3+4) \times 100 \div 2 = 350m$

D = $(2+3) \times 200 \div 2 = 500m$

E = $50 \times 2 \div 2 = 500m$

add them up

100

100

800

1800

1800

(b) Write down the average horizontal acceleration of the drone.

gradient from
$$(0,0)$$
 to $(600,0)$

$$= 0 \qquad \qquad 0 \qquad \qquad 0 \qquad \qquad m/s^2 \qquad \qquad [1]$$
[Total 4 marks]

answes

Leave blank

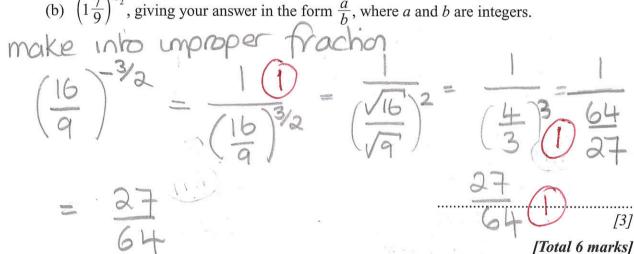
15 Find the value of:

(a) $\frac{10}{\sqrt{5}}$, giving your answer in the form \sqrt{c} , where c is an integer.

$$\frac{10}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{1000}{5} = 200$$

$$\Rightarrow 2 = \sqrt{4} \Rightarrow \sqrt{4} \times \sqrt{5} = \sqrt{20}$$

(b) $\left(1\frac{7}{9}\right)^{-1\frac{1}{2}}$, giving your answer in the form $\frac{a}{b}$, where a and b are integers.



The table shows a list of metals and their densities (in g/cm³).

Name of metal	Density (g/cm³)
Aluminium	2.7
Iron	8
Silver	10.5

11



Leave

blank

A metal of volume 0.5 m³ has a mass of 4000 kg. Which metal do you think this is? Show your working.

orking.
$$10000000 \text{ cm}^3$$
 = 10000000 cm^3 $0.5\text{m}^3 = 5000000000$ $400000 = 400000000$

GCSE Maths / Higher / Set 1 / Paper 1



[Total 2 marks]

All shorts are reduced by 10% and all jeans are reduced by 20%.

The ratio of the original price of jeans to the original price of shorts is 7:5. The sale price of the shorts is £18.00.

What is the sale price of the jeans?

:.
$$jeans = 7x4$$

= $f28 (m1)$



[Total 4 marks]

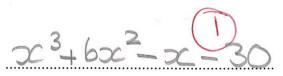
18 Expand and simplify (x+3)(x+5)(x-2)

$$(x+3)(x+5) = x^2 + 3x + 5x + 15$$

= $x^2 + 8x + 15$

$$(x-2)(x^2+8x+15)$$

 $x^3+8x^2+15x-2x^2-16x-30$

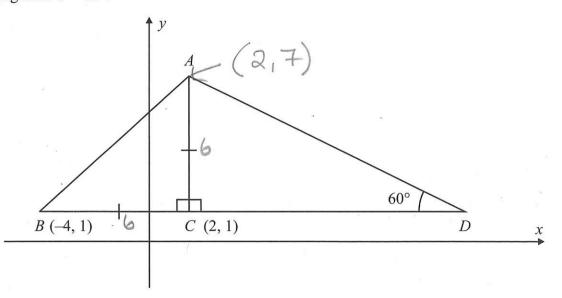


[Total 3 marks]

Leave blank

On a coordinate grid, B = (-4, 1) and C = (2, 1). Triangle ABC is isosceles. Angle $ADC = 60^{\circ}$.

Leave blank



(a) Find an expression for the exact length of CD. Give your answer in the form $a\sqrt{b}$, where a and b are integers.

$$\tan 60 = \frac{60}{CD}$$

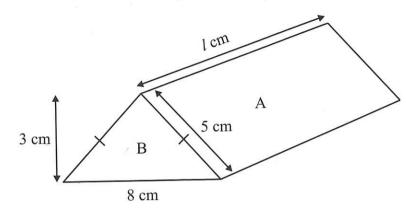
$$CD = 2 \sqrt{3}$$

(b) Find an expression for the exact length of AD. Give your answer in its simplest form.

$$A0^2 = 36 + 12 = 48$$

$$AD = 4\sqrt{3}$$

The ratio of the pressures exerted on the ground when the prism is stood on face A to when it is stood on face B is 3:5.



Find the missing length, l.

force is the same

area
$$d A = 5 \times L = 5L$$

area $d B = 3 \times 8 \div 2 = 12 \text{ cm}^3 \text{ }$

Pressure of face $A = \frac{3}{5}$ of pressure of face B(1): area of A must be $\frac{5}{3} \times bigger$

14

$$l = \frac{1}{2}$$
 cm

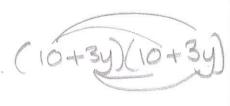
[Total 4 marks]

Leave blank 21 (a) Solve the simultaneous equations

$$x^2 + y^2 = 20$$

$$x - 3y = 10$$

$$(x = 10 + 3y)^2 + y^2 = 200$$



Leave

blank

$$y^2+100+30y+30y+9y^2=20$$

$$y+9y^2+60y+100=20$$

$$10y^2 + 60y + 80 = 0(1)$$

$$y = \frac{10 + 3x}{2} + 0$$

$$x =$$
 $y =$

$$x = \dots \qquad y = \dots$$

(b) How many points of intersection are there for the graphs with equations $x^2 + y^2 = 20$ and x - 3y = 10? Explain your answer.

The graphs will have 2 bonks of into-sochion as they are

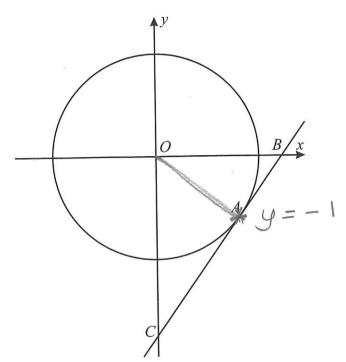
guadratic simultaneous

[1]

[Total 6 marks]

GCSE Maths / Higher / Set 1 / Paper 1

The diagram shows a sketch of the circle with equation $x^2 + y^2 = 5$. The *v*-coordinate of point A is -1. The tangent to the circle at A crosses the axes at B and C as shown.

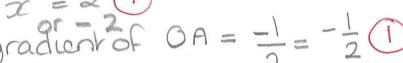


Find the area of triangle *OBC*.

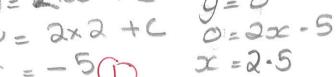
$$x^2 + y^2 = 5$$

$$y = -1$$
 $x^2 + (-1)^2 = 5$

$$\chi^2 = 4$$



gradient of $CB = \frac{1}{2} = -\frac{1}{2}$ (perpendicular to CA) y = 2xx + C y = 2x + C y = 2x



area = 2.5×5 -2

[Total 5 marks]

 $[TOTAL\ FOR\ PAPER = 80\ MARKS]$





General Certificate of Secondary Education

GCSE **Mathematics (Grade 9-1) Higher Tier**

er			
	er	er	er

Practice Set 1 Paper 1: Non-calculator

Time allowed: 1 hour 30 minutes

Surname	-	
Other names	9	*
Candidate signature		

In addition to this paper you should have:

- A pen, pencil and eraser.
- · A ruler.
- · A protractor.
- · A pair of compasses.

Calculators may not be used.



Instructions to candidates

- Write your name and other details in the spaces provided above.
- Answer all questions in the spaces provided.
- In calculations show clearly how you worked out your answers.
- Diagrams are **not** drawn accurately unless otherwise indicated.

Information for candidates

- There are 80 marks available for this paper.
- The marks available are given in brackets at the end of each question.
- · You may get marks for method, even if your answer is incorrect.

Advice to candidates

- Work steadily through the paper.
- Don't spend too long on one question.
- If you have time at the end, go back and check your answers.

I	or exam	iner'	s use
Q	Mark	Q	Mark
1		12	
2		13	-
3		14	
4		15	
5		16	
6		17	7
7		18	
8		19	
9		20	
10		21	-
11		22	
Tota	ıl		

You must show all of your working.

a and **b** are column vectors such that $\mathbf{a} = \begin{pmatrix} 8 \\ 3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} 1 \\ -7 \end{pmatrix}$. Calculate:

(a) 3**a**

[1]

(b) $\mathbf{a} - 4\mathbf{b}$

[2]

[Total 3 marks]

2 140% of x is 28. Find the value of x.

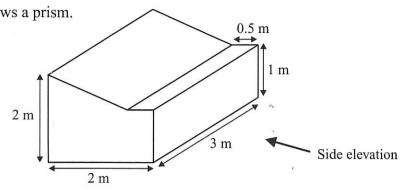
GCSE Maths / Higher / Set 1 / Paper 1

x =

[Total 2 marks]

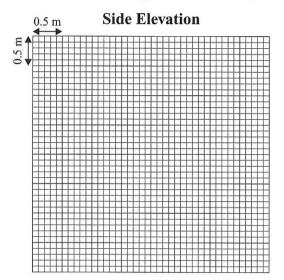
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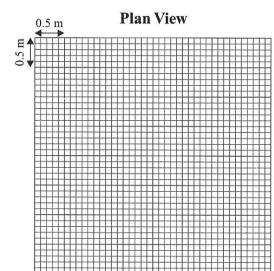
The diagram shows a prism.



3

Using the scale shown on the grids, accurately draw the side elevation and plan view of the prism.





[Total 2 marks]

Leave

blank

4 (a) Make y the subject of the formula x = 3y - 5

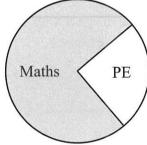
[2]

(b) Factorise the expression $8x^2 - 12xy$

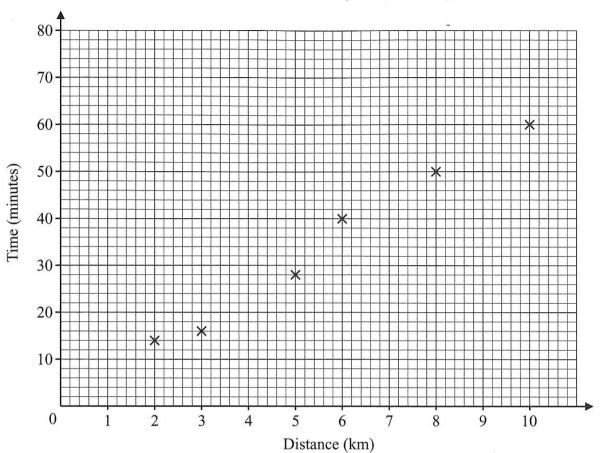
[Total 4 marks]

The sets ξ , P and Q are shown below. $\xi = \{\text{positive integers less than or equal to 20}\}$ $P = \{ prime numbers \}$ $Q = \{1, 2, 3, 4, 6, 8, 12\}$ (a) List the members of the set $P \cap Q$ (b) Find $n(P \cup Q)$ [Total 4 marks] Mathilde asks her group of friends whether they like Maths, PE

or History lessons the most. She puts her results in a pie chart.



She claims that, "No one in my school likes History the most." Do you agree with her statement? Explain your answer. [Total 1 mark] Leave blank Dom has been training for a half marathon. He records the distances and times taken when he goes out running.



(a) Dom also completed a 4 km run in 21 minutes and a 9 km run in 62 minutes. Plot these points on the graph.

[1]

(b) Use the graph to estimate how long it would take him to run 7.5 km.

 minutes
[2]

(c) Why might you not expect the points to lie in a straight line?

5

[Total 4 marks]

Leave

blank

8	Alice has 2 dogs, Ollie and Taffy. Ollie eats $\frac{2}{3}$ of a tin of dog food every day and Taffy eats $\frac{2}{5}$ of a tin every day. Alice buys a crate of 24 tins.
	How many whole days should the crate last?

Leave blank

..... days [Total 3 marks]

Look at this calculation.

GCSE Maths / Higher / Set 1 / Paper 1

 $\frac{226\times0.074}{0.681}$

(a) By rounding each number to 1 significant figure, work out an estimate to the calculation.

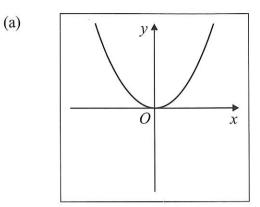
(b) Explain whether you think your answer to part (a) is an overestimate, underestimate or if it is impossible to tell.

[1]

[Total 3 marks]

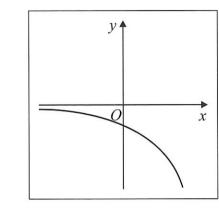
© CGP 2016 — copying more than 5% of this paper is not permitted Choose an equation from the box to match each of the graphs below.

 $y = x^2$ $y = -x^3$ $y = \sin x$ $y = \cos x$ $y = \frac{1}{x}$ $y = 2^{x}$ $y = -2^{x}$



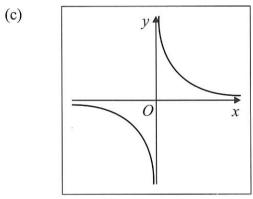
Leave

blank

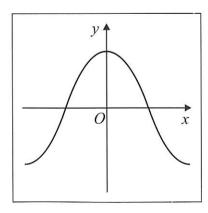


(b)

y = [1]



[1]



7

[1]

[Total 4 marks]

(d)

11 A child's set of building blocks contains 5 different colours. One block is selected at random.

Leave blank

The table shows the probabilities of selecting a blue block and a green block.

Block Colour	Blue	Green	Orange	Red	Yellow
Probability	0.2	0.35			

The probability of picking out a green or orange block is 0.62 The probability of picking out a block that is not yellow is 0.92

Complete the table to show the probability of picking each block colour.

[Total 3 marks]

- Two numbers are in the ratio 4:5. Their highest common factor is 16.
 - (a) Find a possible pair of numbers.

	and
(b)	Are there any other possible pairs? Explain your answer.
	[1]

13 ABC and DEF are parallel. AG and BF are parallel. AE = BE = EFAngle $DEG = 46^{\circ}$

B

Find the size of the angles marked p and q. You must show your working.

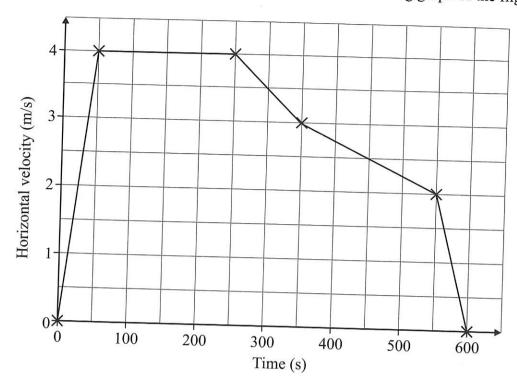
p =

Leave

blank

[Total 3 marks]

Nuala flew her drone at the beach for 10 minutes. The drone automatically recorded its horizontal velocity and Nuala was able to generate the following graph of the flight.



(a) Use the graph to work out the total horizontal distance covered by the drone.

10

 m
[3]

(b) Write down the average horizontal acceleration of the drone.

[1]

[Total 4 marks]

Leave	,
blank	

15 Find the value of:

(a) $\frac{10}{\sqrt{5}}$, giving your answer in the form \sqrt{c} , where c is an integer.

		•	•		•	•		•		•						•			•	•	•		9			
																					l	1		3	1	7

Leave

blank

(b) $\left(1\frac{7}{9}\right)^{-1\frac{1}{2}}$, giving your answer in the form $\frac{a}{b}$, where a and b are integers.

[Total 6 marks]

The table shows a list of metals and their densities (in g/cm³).

Name of metal	Density (g/cm ³)	
Aluminium	2.7	
Iron	8	
Silver	10.5	

A metal of volume 0.5 m³ has a mass of 4000 kg. Which metal do you think this is? Show your working. 17 There is a sale on at a clothes shop. All shorts are reduced by 10% and all jeans are reduced by 20%.

The ratio of the original price of jeans to the original price of shorts is 7:5. The sale price of the shorts is £18.00.

What is the sale price of the jeans?

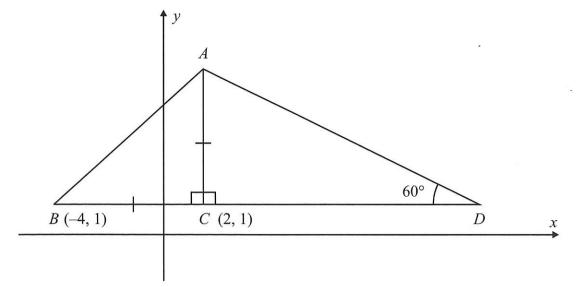
[Total 4 marks]

Expand and simplify (x + 3)(x + 5)(x - 2)

[Total 3 marks]

- Leave blank
- 19 On a coordinate grid, B = (-4, 1) and C = (2, 1). Triangle ABC is isosceles. Angle $ADC = 60^{\circ}$.

Leave blank



(a) Find an expression for the exact length of CD. Give your answer in the form $a\sqrt{b}$, where a and b are integers.

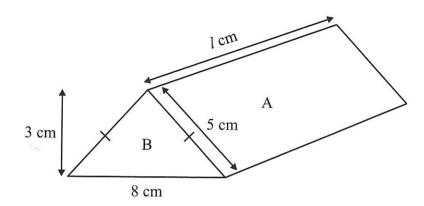
(b) Find an expression for the exact length of AD. Give your answer in its simplest form.

$$AD = \dots$$

[Total 6 marks]

20 The triangular prism below has length l cm.

The ratio of the pressures exerted on the ground when the prism is stood on face A to when it is stood on face B is 3:5.



Find the missing length, *l*.

l	=	 cm
		 CIII

[Total 4 marks]

Leave	
blank	

21 (a) Solve the simultaneous equations

$$x^2 + y^2 = 20$$

$$x - 3y = 10$$

 $x = \dots \qquad y = \dots$

 $x = \dots$ $y = \dots$ [57]

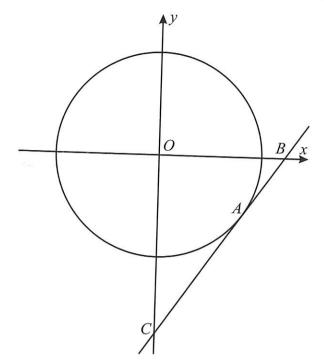
(b) How many points of intersection are there for the graphs with equations $x^2 + y^2 = 20$ and x - 3y = 10? Explain your answer.

15

[Total 6 marks]

[1]

Leave blank The diagram shows a sketch of the circle with equation $x^2 + y^2 = 5$. The y-coordinate of point A is -1. The tangent to the circle at A crosses the axes at B and C as shown.



Find the area of triangle OBC.

[Total 5 marks]

[TOTAL FOR PAPER = 80 MARKS]

Leave blank



General Certificate of Secondary Education

GCSE Mathematics (Grade 9-1) Higher Tier

Centre name			
Centre number			,
Candidate number			

Practice Set 1 Paper 1: Non-calculator

Surname	N
Other names	
Candidate signature	

Time allowed: 1 hour 30 minutes

In addition to this paper you should have:

- · A pen, pencil and eraser.
- A ruler.
- · A protractor.
- · A pair of compasses.

Calculators may not be used.



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- Answer all questions in the spaces provided.
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- You may get marks for method, even if your answer is incorrect.

Advice to candidates

- Work steadily through the paper.
- Don't spend too long on one question.
- If you have time at the end, go back and check your answers.

For examiner's use			
Q	Mark	Q	Mark
1		12	
2		13	
3		14	
4		15	(X.
5		16	
6		17	
7		18	(gr)
8		19	
9	•	20	
10		21	
11		22	
Tota	l		